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Phase transition in the two-dimensional dipolar planar rotator model

L A S Mól^{1,2} and B V Costa²

¹ Departamento de Física, Universidade Federal de Viçosa, 36570-000, Viçosa, Minas Gerais, Brazil

² Departamento de Física, Laboratório de Simulação, ICEX, UFMG, Caixa Postal 702, 31270-901, Belo Horizonte, MG, Brazil

E-mail: lucasmol@ufv.br

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Abstract

In this work we have used extensive Monte Carlo simulations and finite size scaling theory to study the phase transition in the dipolar planar rotator model (dPRM), also known as dipolar XY model. The true long-range character of the dipolar interactions was taken into account by using the Ewald summation technique. Our results for the critical exponents do not fit those from known universality classes. We observed that the specific heat is apparently non-divergent and the critical exponents are $\nu = 1.277(2)$, $\beta = 0.2065(4)$ and $\gamma = 2.218(5)$. The critical temperature was found to be $T_c = 1.201(1)$. Our results are clearly distinct from those of a recent renormalization group study from Maier and Schwabl (2004 *Phys. Rev. B* **70** 134430) and agrees with the results from a previous study of the anisotropic Heisenberg model with dipolar interactions in a bilayer system using a cut-off in the dipolar interactions (Mól and Costa 2009 *Phys. Rev. B* **79** 054404).

(Some figures in this article are in colour only in the electronic version)

1. Introduction

The planar rotator model (PRM) in two dimensions, also known as the XY model, is known to have a critical line in the low temperature region [1–3]. The PRM is described by the following Hamiltonian: $H = -J \sum_{\langle i,j \rangle} \vec{S}_i \cdot \vec{S}_j = -J \sum_{\langle i,j \rangle} (S_i^x S_j^x + S_i^y S_j^y)$, where \vec{S}_i is a two-dimensional vector (S_i^x, S_i^y) defined in the sites i of a two-dimensional lattice and $\langle i, j \rangle$ means that the summation is to be evaluated for nearest neighbor sites. As a prototype the PRM is expected to describe the magnetic properties of ferromagnetic thin films where the spins lie in the film plane. Although very simple, this model presents some unusual characteristics, such as the absence of spontaneous magnetization for any $T > 0$, which is a consequence of the Mermin and Wagner theorem [4]. Thus, the system cannot have a phase transition of the order–disorder type; nevertheless, there is still a phase transition in the model characterized by a change in the spin–spin correlation function behavior. An algebraic decay of the correlation function is observed below a characteristic temperature, T_{BKT} , above which the decay is exponential. Besides that, the correlation

length is expected to diverge exponentially as long as T_{BKT} is approached from above, i.e. $\xi(r) \sim a \exp(b/\sqrt{T - T_{\text{BKT}}})$ for $T > T_{\text{BKT}}$, while it remains infinity for any $T < T_{\text{BKT}}$. This transition is called the Berezinskii–Kosterlitz–Thouless (BKT) phase transition [2, 3]. Several works, analytical as well as numerical, dealing with the subject have been published since the seminal work of Berezinskii and Kosterlitz and Thouless [5–9]. Besides that, it is also observed that the specific heat does not diverge; instead, it has a broad maximum at a temperature slightly higher than T_{BKT} [10–13]. There are two interpretations for the mechanism leading to this transition: Berezinskii [2] and Kosterlitz and Thouless [3] assume that it is driven by a vortex–anti-vortex unbinding mechanism, while Patrascioiu and Seiler [14] were able to obtain the critical temperature and predicted the existence of a phase transition in the Coulomb gas in any dimension ($d > 1$) by considering that the mechanism responsible for the transition is a polymerization of domain walls. (As a matter of unification of terminology we use in this paper the label BKT for this kind of transition.)

However, in order to achieve a deeper insight into the magnetic properties of thin films, one has to include dipolar

interactions between the magnetic moments of the lattice. This inclusion changes the scenario drastically, as discussed by Maleev [15]. The long-range dipolar interactions stabilize the magnetization at low temperatures in such a way that an order–disorder phase transition is now expected to take place. In a recent paper, Maier and Schwabl [16] analyzed the phase transition in the dipolar planar rotator model (dPRM) by using renormalization group techniques. Their results indicate that the dPRM belongs to a new universality class characterized by an exponential behavior of the magnetization, susceptibility and correlation length. Besides that, the specific heat was found to be non-divergent, as occurs in the BKT phase transition. In this work, we have used extensive Monte Carlo simulations to study phase transition in the dPRM. Our results clearly indicate that the transition is of the order–disorder type and is characterized by a non-divergent specific heat and unusual critical exponents.

2. Dipolar planar rotator model and the Monte Carlo method

The model we are interested in consists of a square lattice with dimension $L \times L$. At each site we place a classical spin variable $\vec{S}_i = (S_i^x, S_i^y)$ with $\vec{S}_i^2 = 1$. The interactions are defined by the following Hamiltonian:

$$H = -J \sum_{\langle i,j \rangle} \vec{S}_i \cdot \vec{S}_j + D \sum_{i \neq j} \left[\frac{\vec{S}_i \cdot \vec{S}_j}{r_{ij}^3} - \frac{3(\vec{S}_i \cdot \vec{r}_{ij})(\vec{S}_j \cdot \vec{r}_{ij})}{r_{ij}^5} \right]. \quad (1)$$

Here, $J > 0$ defines a ferromagnetic exchange constant and D is the dipolar constant. \vec{r}_{ij} connects sites i and j while $\langle i, j \rangle$ means that the first summation is evaluated for nearest neighbors only. For the dipolar interactions the summation is evaluated over all pairs $i \neq j$. Periodic boundary conditions have been used in the film plane (x and y directions) while open boundary conditions were applied in the z direction. Ewald summation techniques [17, 18] have been used to take into account the true long-range character of the dipolar interactions³. In all simulations we have assumed $J = 1$ and $D = 0.1$ and for these values only ferromagnetic configurations were found in the low temperature regime. In this work the energy is measured in units of JS^2 and temperature in units of JS^2/k_B .

Our Monte Carlo procedure consists of a simple Metropolis algorithm [19, 20] where one Monte Carlo step (MCS) consists of an attempt to assign a new random direction to each spin in the lattice. To equilibrate the system we have used $100 \times L^2$ MCSs which has been found to be sufficient to reach equilibrium, even in the vicinity of the transition. In our scheme, two sets of simulations have been performed. In the first one, we preliminarily explored the thermodynamic behavior of the model in order to estimate the position of the maxima of the specific heat and susceptibilities and the crossings of the fourth order Binder cumulant. In this first approach we used lattice sizes in the interval $20 \leq L \leq 50$.

³ The Ewald summation allows one to evaluate the dipolar energy without cutoffs, and details about this method can be found in [17, 18].

Once the possible transition temperature is determined, we refined the results by using single and multiple histogram methods [21, 22]. We produced the histograms for each lattice size in the interval $20 \leq L \leq 120$ and they were built at/close to the estimated critical temperatures corresponding to the maxima and/or crossing points obtained in step 1. Details of the histogram techniques can be found in [21, 22].

3. Thermodynamic quantities and finite size scaling theory

We have devoted our efforts to determine a number of thermodynamic quantities, namely the specific heat, magnetization, susceptibility, fourth order Binder cumulant and moments of magnetization as described below. The specific heat is defined as

$$c_v = \frac{\langle E^2 \rangle - \langle E \rangle^2}{Nk_B T^2}, \quad (2)$$

where E is the internal energy of the system (computed using equation (1)) and $N = L^2$ is the lattice volume. The magnetization is

$$M = \frac{1}{N} \langle m \rangle, \quad (3)$$

where

$$m = \sqrt{\left(\sum_{i=1}^N S_i^x \right)^2 + \left(\sum_{i=1}^N S_i^y \right)^2}. \quad (4)$$

The susceptibility is defined by the magnetization fluctuations as

$$\chi_{xy} = \frac{\langle m^2 \rangle - \langle m \rangle^2}{Nk_B T}. \quad (5)$$

The fourth order Binder cumulant reads

$$U_4 = 1 - \frac{\langle m^4 \rangle}{3\langle m^2 \rangle^2}. \quad (6)$$

In order to calculate the critical exponent ν , we also define the following moments of the magnetization [23]:

$$V_1 \equiv 4[m^3] - 3[m^4], \quad (7a)$$

$$V_2 \equiv 2[m^2] - [m^4], \quad (7b)$$

$$V_3 \equiv 3[m^2] - 2[m^3], \quad (7c)$$

$$V_4 \equiv (4[m] - [m^4])/3, \quad (7d)$$

$$V_5 \equiv (3[m] - [m^3])/2, \quad (7e)$$

$$V_6 \equiv 2[m] - [m^2], \quad (7f)$$

where,

$$[m^n] \equiv \ln \left| \frac{\partial \langle m^n \rangle}{\partial T} \right|. \quad (8)$$

In critical phenomena the thermodynamic quantities are expect to behave in the vicinity of the phase transition as [20, 24, 25]

$$c_v \sim t^{-\alpha} \quad (9a)$$

$$\chi \sim t^{-\gamma} \quad (9b)$$

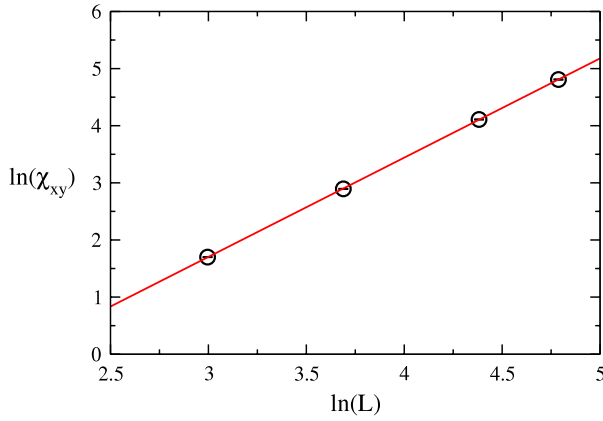


Figure 1. Log–log plot of the maxima of susceptibility as a function of the lattice size for $L = 20, 40, 80$ and 120 . The error bars are shown inside the symbols. The straight line is the best linear fit which gives the exponent $\gamma/\nu = 1.737(1)$.

$$M \sim t^\beta \quad (9c)$$

$$\xi \sim t^{-\nu}, \quad (9d)$$

where $t = |T - T_c|/T_c$ is the reduced temperature, M is the magnetization, ξ is the correlation length and α, β, γ and ν are critical exponents. Although the critical temperature depends on the details of the system under consideration, it is observed that the critical exponents are universal, depending only on a few fundamental factors [20, 24, 25]. The systems are thus divided into a small number of universality classes. Systems belonging to the same universality class share the same critical exponents. Critical exponents are observed to depend only on the spatial dimensionality of the system, the symmetry and dimensionality of the order parameter, and the range of the interactions within the system.

In a finite system like those used in Monte Carlo simulations the divergences in the thermodynamic quantities are replaced by smooth functions. Finite size effects are therefore of great importance in the analysis of the results of Monte Carlo simulations. The theory of finite size scaling [20, 25] provides one way to extract information concerning the thermodynamic limit properties from results obtained in finite systems. The basic assumption of this theory is that in the vicinity of the phase transition the finite size effects should depend on the ratio between the linear dimension of the system and the correlation length, say L/ξ . According to such a theory, specific heat, susceptibility and magnetization for a finite system, in the vicinity of the phase transition, behave as

$$c_v \approx c_\infty(t) + L^{\alpha/\nu} \mathcal{C}(tL^{1/\nu}), \quad (10a)$$

$$\chi \approx L^{\gamma/\nu} \mathcal{X}(tL^{1/\nu}), \quad (10b)$$

$$M \approx L^{-\beta/\nu} \mathcal{M}(tL^{1/\nu}), \quad (10c)$$

where \mathcal{M}, \mathcal{X} and \mathcal{C} are proper derivatives of the free energy. At T_c ($t = 0$) these functions are constants and the size dependences of specific heat, susceptibility and magnetization follow a pure power law. The size dependence of the pseudo-critical temperature, $T_c(L)$, is [20, 25]

$$T_c(L) = T_c + wL^{-1/\nu}, \quad (11)$$

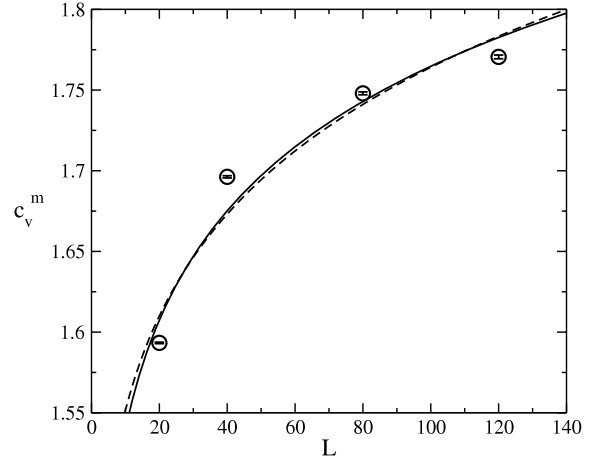


Figure 2. Specific heat maxima as a function of the lattice size. The solid line is the best non-linear fit considering a logarithmic divergence and the dashed line is the best fit considering a power law divergence. The error bars are shown inside the symbols.

where T_c is the critical temperature in the thermodynamic limit. Using the size dependence of the magnetization, equation (10), and the definition of the moments of the magnetization in equation (7), one can easily show that such functions behave as

$$V_j \approx (1/\nu) \ln L + \mathcal{V}_j(tL^{1/\nu}), \quad (12)$$

for $j = 1, 2, \dots, 6$. At $t = 0$ the functions $\mathcal{V}_j(tL^{1/\nu})$ are constants and then the curves for all V_j have the same slope [23] providing a very precise method to determine both the critical exponent ν and the critical temperature.

Concerning the fourth order Binder cumulant, it is expected that its curves should cross at the same point $U^* = U(T = T_c)$ for large enough L . Besides that, its size dependence is expected to obey [26]

$$U_4 \approx U_4(tL^{1/\nu}). \quad (13)$$

4. Results

In the following we show the results obtained by using the histogram method. Each histogram consists of at least 3×10^7 configurations. In figure 1 we show a log–log plot of the maxima of the susceptibility as a function of the lattice size for $L = 20, 40, 80$ and 120 . The data are very well adjusted by a straight line with slope $\gamma/\nu = 1.737(1)$ exhibiting a power law behavior. The specific heat maxima as a function of the lattice size are shown in figure 2. In this figure, the solid line represents the best non-linear adjustment of a logarithmic divergence while the dashed one the best power law divergence adjustment. It is clear that neither of these can adjust our data satisfactorily. This result is similar to that obtained for the PRM without dipolar interactions, and indicates a possible non-divergent specific heat. In figure 3 we show the value of $1/\nu$ for some temperatures obtained by using the moments of the magnetization defined in equations (7) and (12). Using this method we get $T_c^{V_j} = 1.1982(18)$ and $1/\nu = 0.74(2)$.

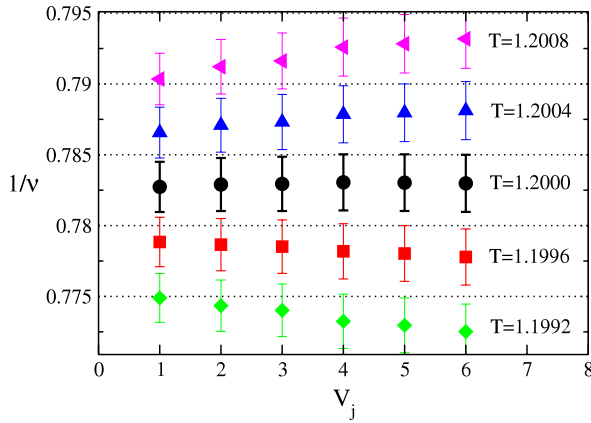


Figure 3. Value of $1/\nu$ obtained by linear fits of V_j versus $\ln(L)$ for each value of j at different temperatures. Note that for $T = 1.2000$ the value of $1/\nu$ is almost the same for all quantities.

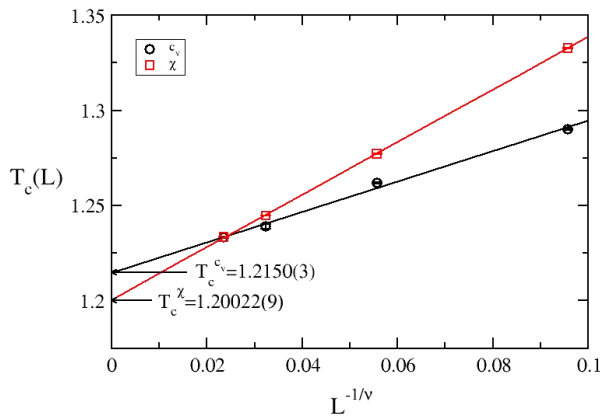


Figure 4. $T_c(L)$ versus $L^{-1/\nu}$. From a linear adjustment we get $T_c^\chi = 1.20022(9)$ and $T_c^{c_v} = 1.2150(3)$.

With the value of $1/\nu$ we may estimate the critical temperature using the finite size scaling properties of the maxima of the susceptibility and specific heat (see equation (11)). In figure 4 we show a plot of $T_c(L)$ as a function of $L^{-1/\nu}$. We obtain $T_c^\chi = 1.20022(9)$ and $T_c^{c_v} = 1.2150(3)$. Using the crossing points of the fourth order Binder cumulant [26] (see figure 5) we estimate the critical temperature $T_c^{U_4} = 1.203(1)$. Our best value for the critical temperature is thus the mean value of the previous estimates $T_c^{U_4}$, $T_c^{V_j}$ and T_c^χ discarding the value obtained by finite size scaling of the specific heat, since its behavior is apparently non-critical. This procedure gives $T_c = 1.201(1)$. Plotting $\ln(M_{xy})$ versus $\ln(L)$ at T_c it is possible to obtain the exponent β/ν . From a linear adjustment we get $\beta/\nu = 0.1617(2)$. In order to verify the validity of our results we show in figures 6–8 the scaling plots of the susceptibility, magnetization and fourth order Binder cumulant according to their finite size scaling functions (see equation (10)). Note that all figures show a very good collapse of the curves for different lattice sizes.

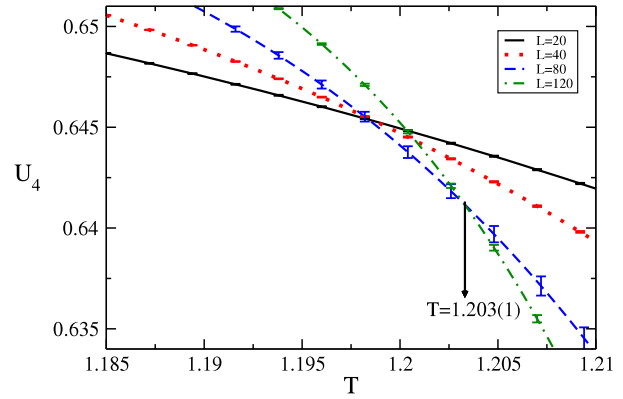


Figure 5. Fourth order Binder cumulant. The critical temperature was estimated by the crossing point of the largest lattice sizes as being $T_c^{U_4} = 1.203(1)$. Only a few error bars are shown for clarity.

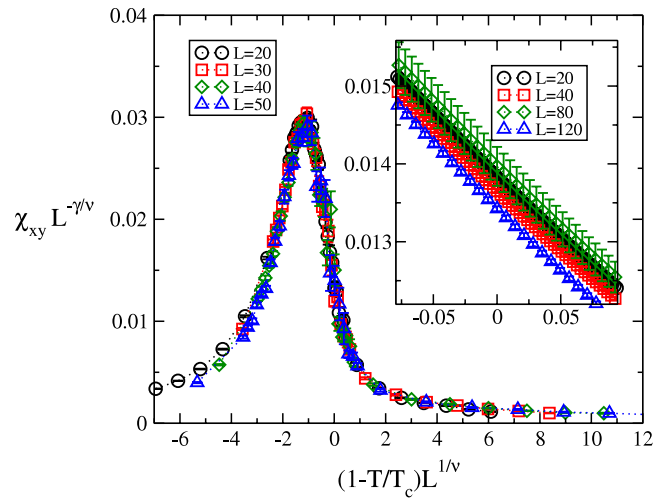


Figure 6. Scaling plot of susceptibility. According to finite size scaling theory [20, 25] the susceptibility is expected to behave as $\chi \approx L^{\gamma/\nu} \mathcal{X}(tL^{1/\nu})$. Note that the curves for different lattice sizes collapse into a single curve. In the outer plot the scaling is done using results from conventional Monte Carlo simulations (step 1) for $L = 20, 30, 40$ and 50 . The inset shows the scaling for the histogram results (step 2 in our simulations) for $L = 20, 40, 80, 120$.

5. Discussion

In this work we have studied the phase transition in the ferromagnetic dipolar planar rotator model (dPRM). Our results indicate that the phase transition in this model is of the order–disorder type and is characterized by the exponents $\nu = 1.277(2)$, $\beta = 0.2065(4)$ and $\gamma = 2.218(5)$ and by a non-divergent specific heat. Our results also indicate that the system has long-range order at low temperatures. This conclusion is based on the following facts: (i) the magnetization for $T < T_c$ does not display a significant decrease as the lattice size is augmented, as for example has been found in Rapini’s work [27] and as expected for a BKT phase transition; (ii) our results are very well described by a finite size scaling theory based on the existence of a low temperature phase with long-range order and finite correlation length [20, 25]. In a BKT phase transition there is no long-range order in the low

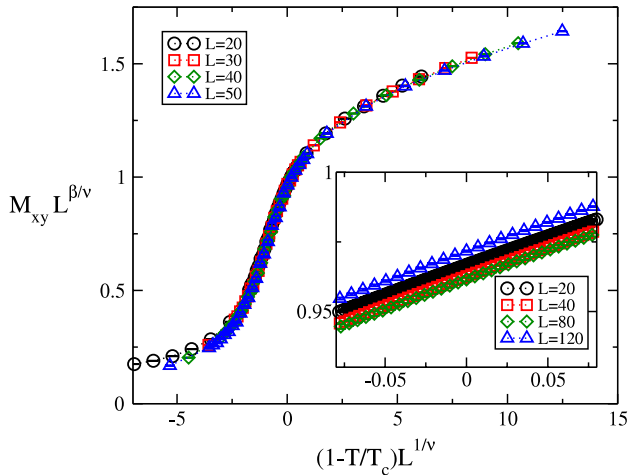


Figure 7. Scaling plot of magnetization. According to finite size scaling theory [20, 25] this quantity is expected to behave as $m \approx L^{-\beta/\nu} \mathcal{M}(tL^{1/\nu})$. Note that the curves for different lattice sizes collapse into a single curve. In the outer plot the scaling is done using results from conventional Monte Carlo simulations (step 1) for $L = 20, 30, 40$ and 50 . The inset shows the scaling for the histogram results (step 2 in our simulations) for $L = 20, 40, 80, 120$.

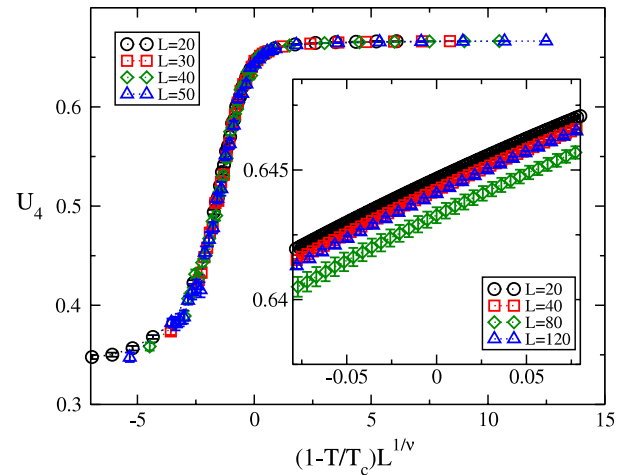


Figure 8. Scaling plot of the fourth order Binder cumulant. According to finite size scaling theory [26] this quantity is expected to behave as $U_4 \approx \mathcal{U}_4(tL^{1/\nu})$. Note that the curves for different lattice sizes collapse into a single curve. In the outer plot the scaling is done using results from conventional Monte Carlo simulations (step 1) for $L = 20, 30, 40$ and 50 . The inset shows the scaling for the histogram results (step 2 in our simulations) for $L = 20, 40, 80, 120$.

temperature phase as a consequence of the Mermin–Wagner theorem [4]. Indeed, the results of Maleev [15] predict the existence of long-range order at low temperatures in the dPRM and our results are consistent with this scenario.

As discussed earlier, recent results by Maier and Schwabl [16] have predicted that this system may belong to a new universality class, characterized by the presence of long-range order at low temperatures and by an exponential behavior of thermodynamic quantities in the vicinity of the ‘critical’ temperature. By an exponential divergence we mean that the correlation length diverges as the ‘critical’ temperature (T_c) is approached as $\xi \propto \exp(b/\sqrt{(T - T_c)})$, similar to the behavior of the BKT phase transition, while the behavior of other thermodynamic quantities are given by powers of the correlation length. Nevertheless, our results for the dPRM are very well described by power law divergences of thermodynamic quantities. As can be seen in figures 6–8, we obtained a very good collapse of the curves from different lattice sizes for the susceptibility, magnetization and Binder cumulant. These curves show that the critical exponents obtained and the conventional finite size scaling theory, that assumes a power law behavior of thermodynamic quantities, describe the Monte Carlo data accurately, indicating that the phase transition in the dPRM is a conventional order–disorder phenomenon with unusual critical exponents. In order to definitely rule out the possibility of this phase transition being in the new universality class proposed by Maier and Schwabl, we should make a comparison of our Monte Carlo results, using a finite size scaling theory based in their predictions and the conventional finite size scaling theory used here. Unfortunately, it is not very clear in the literature how to obtain a finite size scaling theory for exponential divergences. Using a simple replacement of the correlation length by the lattice size (in a manner similar to that made by Challa and Landau in [28]), which should be the first choice, does not give a good

collapse of the curves, mainly because the determination of the critical temperature is quite imprecise in this case and the collapse of the curves depends appreciably on the value used for the critical temperature. In any case, using values for the critical temperature close to the maxima of the susceptibility we were not able to obtain even a reasonable collapse of the curves.

Once the possibility of this phase transition being in the new universality class proposed by Maier and Schwabl is discarded, some questions arise: (i) Why do renormalization group results not agree with our Monte Carlo simulations? (ii) Is the occurrence of the order–disorder transition due to the long-range character of dipolar interactions or to some other property of this model? A definite answer to these questions may take a very long time to obtain because of the non-trivial characteristics presented by this model. Nevertheless, this study gave us some insight into what is happening. The RG study of Maier and Schwabl [16] is based upon some approximations, for instance the using of a continuous version of dPRM, where the lattice character is lost. Since the dipolar interactions have an intrinsic anisotropy which depends in a complicated manner on the location of each spin in the lattice, the lattice geometry could have a strong effect in the system. The identification and discussion of the finer points of the RG study of the dPRM that cause the discrepancy in the results is beyond the scope of this paper. Concerning the origin of the order–disorder transition the question is even more complicated. The long-range order observed at low temperatures is expected to occur only when full long-range interactions are present. Nevertheless, in a recent study of the anisotropic Heisenberg model in a bilayer system [29] using a cut-off in the dipolar interactions we found the same critical behavior. In fact, the critical exponents found ($\nu = 1.22(9)$, $\gamma = 2.1(2)$ and $\beta = 0.18(5)$) agree within the errors with those found in this study ($\nu = 1.277(2)$, $\beta = 0.2065(4)$)

and $\gamma = 2.218(5)$). This observation indicates that the anisotropic character of dipolar interactions may be the main factor responsible for the observed critical phenomena. Indeed, this observation is not new in the literature. As an example, Fernández and Alonso [30] stated that ‘Anisotropy has a deeper effect on the ordering of systems of classical dipoles in 2D than the range of dipolar interactions’. In this work the authors found that the inclusion of a quadrupolar anisotropy drastically changes the phase transition behavior of a system of classical dipoles. Apparently, in our system the intrinsic anisotropy of dipolar interactions plays an essential role in the determination of the universality class of the dPRM.

The possible new universality class is not surprising. In the theory of critical phenomena [20, 25] it is expected that the critical exponents, and thus the universality classes, depend only on the spatial dimensionality of the system, the symmetry and dimensionality of the order parameter, and the range of the interactions within the system, characteristics not shared by the dPRM and models of well known universality classes. Indeed, for the pure dipolar model on the square lattice Carbognani *et al* [31] have found that the critical behavior is characterized by unusual critical exponents.

Acknowledgments

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References

- [1] Wegner F 1967 *Z. Phys.* **206** 465
 [2] Berezinskii V L 1971 *Sov. Phys.—JETP-USSR* **32** 493

- [3] Kosterlitz J M and Thouless D J 1973 *J. Phys. C: Solid State Phys.* **6** 1181
 [4] Mermin N D and Wagner H 1966 *Phys. Rev. Lett.* **17** 1133
 [5] Minnhagen P 1987 *Rev. Mod. Phys.* **59** 1001
 [6] Hikami S and Tsuneto T 1980 *Prog. Theor. Phys.* **63** 387
 [7] Takeno S and Homma S 1980 *Prog. Theor. Phys.* **64** 1193
 [8] Evertz H G and Landau D P 1996 *Phys. Rev. B* **54** 12302
 [9] Costa J E R and Costa B V 1996 *Phys. Rev. B* **52** 994
 [10] Cuccoli A, Tognetti V and Vaia R 1995 *Phys. Rev. B* **52** 10221
 [11] Gupta R and Baillie C F 1992 *Phys. Rev. B* **45** 2883
 [12] Olson P 1973 *Phys. Rev. Lett.* **73** 3339
 [13] Lima A B and Costa B V 2003 *J. Magn. Magn. Mater.* **263** 324
 [14] Patrascioiu A and Seiler E 1988 *Phys. Rev. Lett.* **60** 875
 [15] Maleev S V 1976 *Sov. Phys.—JETP* **43** 1240
 [16] Maier P G and Schwabl F 2004 *Phys. Rev. B* **70** 134430
 [17] Weis J-J 2003 *J. Phys.: Condens. Matter* **15** S1471
 [18] Wang Z and Holm C 2001 *J. Chem. Phys.* **115** 6351
 [19] Metropolis N, Rosenbluth A, Rosenbluth M, Teller A and Teller E 1953 *J. Chem. Phys.* **21** 1087
 [20] Landau D P and Binder K 2005 *A Guide to Monte Carlo Simulations in Statistical Physics* (New York: Cambridge University Press) ISBN 0521842387
 [21] Ferrenberg A M 1991 *Computer Simulation Studies in Condensed Matter Physics III* ed D Landau, K Mon and H Schüttler (Berlin: Springer)
 [22] Ferrenberg A M and Swendsen R H 1989 *Phys. Rev. Lett.* **63** 1195
 [23] Chen K, Ferrenberg A M and Landau D P 1993 *Phys. Rev. B* **48** 3249
 [24] Stanley H E 1971 *Introduction to Phase Transition and Critical Phenomena* (Oxford: Clarendon)
 [25] Privman V (ed) 1990 *Finite Size Scaling and Numerical Simulation of Statistical Systems* (Singapore: World Scientific)
 [26] Binder K 1981 *Phys. Rev. Lett.* **47** 693
 [27] Rapini M, Dias R A and Costa B V 2007 *Phys. Rev. B* **75** 014425
 [28] Challa M S S and Landau D P 1986 *Phys. Rev. B* **33** 437
 [29] Mól L A S and Costa B V 2009 *Phys. Rev. B* **79** 054404
 [30] Fernández J F and Alonso J J 2007 *Phys. Rev. B* **76** 014403
 [31] Carbognani A, Rastelli E, Regina S and Tassi A 2000 *Phys. Rev. B* **62** 1015